

**ALMOST DISJOINT FAMILIES  
UNDER AUTOMORPHISMS OF  $\wp(\mathbb{N})/Fin$  AND  $\ell_\infty/c_0$**

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The talk will be devoted to some properties of almost disjoint families in  $\mathbb{N}$  (AD families, in short) and of related structures: disjoint families and subalgebras in  $\wp(\mathbb{N})/Fin$ , and subspaces of  $\ell_\infty/c_0$  generated by adequate characteristic functions. We are interested in the existence of (different kinds of) automorphisms which send one AD family of a given cardinality  $\kappa < \mathfrak{c}$  onto another one. It is well-known that for certain AD families of cardinality  $\aleph_1$  there is no Boolean automorphism of  $\wp(\mathbb{N})/Fin$  with such property. We will first discuss the reasons behind that. Then we will see how we can consider an AD family as a subset of  $\ell_\infty$  or its quotient  $\ell_\infty/c_0$ , and how the situation is different here. In contrast to the Boolean case, the existence of a pair of AD families of cardinality  $\kappa < \mathfrak{c}$  that does not admit any Banach automorphism of  $\ell_\infty/c_0$  which sends one of them onto another depends on additional set-theoretic assumptions. The second part of the talk will be based on some results from <https://arxiv.org/abs/2509.22376>, which is a joint work with Piotr Koszmider.